

MATH 203
Differential & Integral Calculus I
Winter 2020

Instructor*: _____

Office/Tel No.: _____

Office Hours: _____

*Students should get the above information from their instructor during class time. The instructor is the person to contact should there be any questions about the course.

Textbook: *Thomas' Calculus: Early Transcendentals, Single Variable, (ed. 14) Books a la Carte edition plus MyLab Math, (Pearson).*

Prerequisite: Math 201 or an equivalent Functions course.

Pre-test: A pre-test is posted on the Meta Moodle site of this course to help students determine if their prerequisite mathematical background is strong enough to take this course. Students are encouraged to go to the Meta site, click on *README: About the Pre-test* and then take the test itself to see where they stand. The results of the test may be used by the course coordinators to advise students on what remedial actions they can take if they perform poorly on this pre-test.

Office Hours: Your professor will announce her/his office hours during which she/he will be also available to give a reasonable amount of help. Note, however, that if you missed a class it is not reasonable to expect your professor to cover the missed material for you.

Tutorials: The material in this course requires a lot of practice. There is not enough class time to do all the examples and problems needed to learn the material thoroughly. The Department has therefore organized special tutorial sessions conducted every week to provide additional support to students outside the lecture room environment. These sessions are conducted by tutors who will help with solving problems on the topics learned in class that week, with particular emphasis on the material that students may have difficulties with in this course. Tutorials are an important resource to help you succeed in this course and students are strongly encouraged to participate and be active at these problem-solving sessions.

As an added incentive, several quizzes will be given during the tutorials, and up to five bonus marks will be added to your final mark from the quizzes.

Math Help Centre: In addition to Tutorials, a Math Help Centre staffed by graduate students is available. The schedule of its operation and its location will be posted in the Department and on the Department webpage (<https://www.concordia.ca/arts/math-stats/services/math-help-centre.html>).

WeBWorK: Every student will be given access to an online system called **WeBWorK**. The system provides you with many exercises. Students will use this system to do online assignments (see **Assignments** below). In addition, before the midterm test and before the final exam, practice problems will be posted in **WeBWorK** to help you review the material of the course.

MyLabMath: Every student who purchases the loose-leaf version of the textbook will be given access to one more online system called **MyLabMath**. This system contains an e-version of the textbook, as well as a large number of various resources, like practice exercises, typical examples on different topics, often with solutions, video materials, etc., that help you master the course material.

Assignments: Students are expected to submit assignments online using **WeBWork**. Late assignments **will not** be accepted. Assignments contribute 10% to the final grade. Working regularly on the assignments is essential for success in this course. Students are also strongly advised to do as many problems as their time permits from the list of recommended problems included in this outline, as well as work on the practice exercises in **WeBWork** and in **MyLabMath**.

Calculators: Only calculators approved by the Department (with a sticker attached as a proof of approval), such as **Sharp EL 531** or the **Casio FX 300MS**, available at the Concordia Bookstore, are permitted for the class test and final examination. See <https://www.concordia.ca/content/dam/artsci/math-stats/docs/AppCalculatorList.pdf> for a list of Approved and Not-approved calculators.

Midterm Test: There will be one **midterm test**, based on the material of weeks 1-6, which will contribute up to 25% to your final grade (see the **Grading Scheme** below). The test will be **common** for all sections of this course and will be held on **Sunday March 8, 2020, at 14:00 (i.e. 2:00 P.M.)**. **Note that the time changes that day.** It is the Department's policy that tests missed for any reason, including illness, cannot be made up. If you miss the midterm for any valid reason, e.g. illness, religious, etc., supported by appropriate documentation, the final exam will count for 90% of your final grade, and the assignments will count for the remaining 10%.

Travel arrangements are not considered a valid reason for missing the test.

NOTE: If you are taking another MATH 200 level course with a common midterm test at the same time as this one, you may choose which of the two tests you want to write. You must then inform the instructor of the other course that you will not write that test because of the time conflict between the two courses. In this case, the 90%-10% formula will apply to that other course.

Final Exam: The final examination will be three hours long and will cover all the material in the course. NOTE: Students are responsible for finding out the date and time of the final exams once the schedule is posted by the Examinations Office. Conflicts or problems with the scheduling of the final exam must be reported directly to the Examinations Office, not to your instructor.

Grading Scheme: The final grade will be based on the higher of (a) or (b) below:
a) 10% for the assignments, 25% for the midterm test, 65% for the final exam.
b) 10% for the assignments, 10% for the midterm test, 80% for the final exam.

Up to 5 bonus marks will be added from the quizzes (see **Tutorials**).

IMPORTANT: PLEASE NOTE THAT THERE IS NO "100% FINAL EXAM" OPTION IN THIS COURSE.

Academic Integrity and the Academic Code of Conduct

This course is governed by Concordia University's policies on Academic Integrity and the Academic Code of Conduct as set forth in the Undergraduate Calendar and the Graduate Calendar. Students are expected to familiarize themselves with these policies and conduct themselves accordingly. "Concordia University has several resources available to students to better understand and uphold academic integrity. Concordia's website on academic integrity can be found at the following address, which also includes links to each Faculty and the School of Graduate Studies: concordia.ca/students/academic-integrity." [*Undergraduate Calendar, Sec 17.10.2*]

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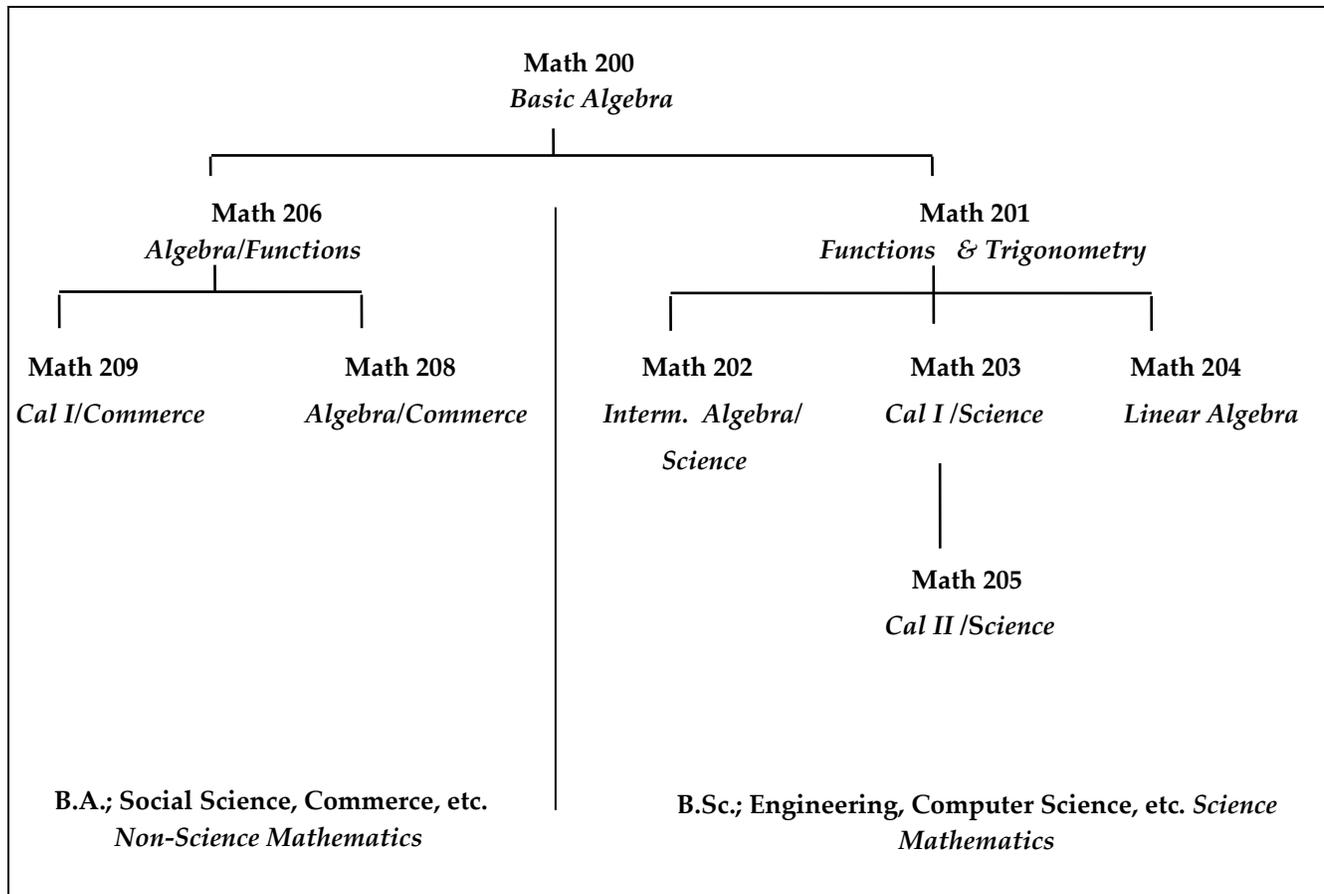
Note: All of Chapter 1 is a review of material that is covered in prerequisite courses, and is important for this course. The material that is skipped in this review will be introduced briefly later in the course when needed. If you don't know this preliminary material thoroughly, it is particularly important that you learn it through the assignment questions and recommended problems. If you still feel you don't know it well enough after the first class or so (you should also try the quiz at the very end of this document) you may want to consider dropping the course and taking MATH 201 instead.

Weeks	Topics	Recommended Problems
1	1.1 Representations of Functions	p.11: 3, 5, 7, 9, 13, 21, 23, 27, 49, 51
	1.2 Combining Functions; Shifting & Scaling Graphs	p.18: 1, 3, 5, 7, 9, 15, 17, 19, 21, 23, 25
	1.3 Trigonometric Functions	p.27: 7, 9, 11, 15, 19, 25, 29, 37, 41, 47, 49
2	1.5 Exponential Functions	p.37: 3, 7, 9, 11, 13, 15, 21, 25, 27, 33
	1.6 Inverse Functions and Logarithms	p.49: 9, 17, 21, 29, 31, 41, 47, 53, 61, 63, 71
3	2.1 Rates of change and Tangent Lines	p.61: 1, 3, 5, 23, 25
	2.2 Limit of a Function and Limit Laws	p.71: 3, 5, 13, 15, 19, 25, 27, 35, 37, 55, 65
	2.4 One-Sided Limits	p.88: 3, 7, 9, 15, 17, 19, 33, 37
	2.6 Limits Involving Infinity; Asymptotes	p.112: 1, 9, 11, 21, 27, 35, 41, 69, 71, 87, 89
4	2.5 Continuity	p.100: 5, 13, 19, 29, 31, 41, 45, 49, 61
	3.1 Tangent Lines and the Derivatives	p.123: 5, 11, 17, 21, 25, 31, 33
	3.2 The Derivative as a Function	p.130: 3, 9, 11, 17, 23, 25, 55, 59
5	3.3 Differentiation rules	p.142: 5, 7, 11, 15, 21, 23, 29, 43, 47, 61
	3.4 The Derivative as a Rate of Change	p.150: 5, 7, 9, 13, 15, 19, 23
6	3.5 Derivatives of Trigonometric Functions	p.158: 3, 7, 11, 13, 19, 23, 31, 37
	3.6 The Chain Rule	p.166: 5, 7, 13, 21, 23, 31, 35, 37, 45, 63, 77
7	3.7 Implicit differentiation	p.172: 1, 5, 11, 15, 25, 27, 37, 39, 41
	3.8 Derivatives of Inverse Functions and Logs	p.183: 7, 11, 27, 31, 33, 37, 39, 51, 53, 89, 95
8	3.9 Inverse Trigonometric Functions (start with the review of inverse sin & cos, § 1.6)	p.189: 5, 9, 11, 17, 25, 29, 39, 43, 45
	3.10 Related rates	p.196: 7, 11, 13, 15, 17, 21, 23, 27, 31, 33, 39
	3.11 Linearization and Differentials	p.209: 5, 11, 17, 19, 23, 33, 39, 45, 49, 55, 59
9	4.1 Extreme Values of Functions on Intervals	p.227: 5, 17, 23, 31, 37, 39, 53, 63, 69, 89
10	4.2 Mean Value Theorem	p.235: 5, 11, 13, 21, 25, 27, 29, 61, 63, 65
	4.5 Indeterminate forms and L'Hôpital's Rule	p.262: 9, 11, 15, 17, 21, 43, 47, 51, 53, 61, 63
11	4.3 Monotonic Functions	p.241: 5, 7, 19, 27, 29, 54, 57, 61
	4.4 Concavity and Curve Sketching	p.251: 5, 9, 13, 17, 31, 37, 43, 63, 81, 85, 99
12	4.6 Applied Optimization	p.269: 3, 5, 7, 9, 11, 13, 15, 19, 29, 37, 39, 41
13	REVIEW	

Choosing Between Math 201 and Math 203

If the last math course you took was at the high school level (Quebec), and more than five years have passed since, you should probably register for Math 200. If you are still unsure of your level, read on.

Math Courses at Concordia



A self-administered test to help you decide between Math 201 and Math 203 follows. Give yourself about 30 minutes to complete the test. Be honest with yourself, since registering in the wrong course may cost you money and result in a poor grade. Remember that all university-level courses usually demand quite a bit of your time. Students in Math 203 will find they will not have time once the course begins to review material that they are expected to know before they enter the course.

Scoring: 10 or less = Math 201; 11-14 = see an advisor; 15 or better = Math 203. Answers are on the last page.

**MATH 203
Qualifying Test**

1) What is the equation, in *slope-intercept* form, of the line whose slope is 7 and whose *y-intercept* is -3 ?

- a) $y = -3x + 7$ b) $y = 7x - 3$
c) $y = 7x + 21$ d) $y = 7x - 21$
e) $y = -7x + 3$

2) What is the slope of any line *parallel* to the line $5x + 6y = 30$?

- a) $-\frac{6}{5}$ b) $-\frac{5}{6}$ c) 0 d) $\frac{5}{6}$ e) $\frac{6}{5}$

3) The lines $-4x + 5y = -10$ and $5x + ky = 12$ are perpendicular. What is the value of k ?

- a) -5 b) -4 c) 4 d) 5 e) 10

4) Find the coordinates of the *midpoint* M , and the *length* L of the line segment joining the points $(3, -2)$ and $(4, -1)$. Answer in simple radical form.

- a) $M\left(\frac{7}{2}, -\frac{3}{2}\right)$, $L = \sqrt{2}$ b) $M\left(\frac{7}{2}, \frac{3}{2}\right)$, $L = \sqrt{3}$ c) $M\left(\frac{1}{2}, -\frac{1}{2}\right)$, $L = \sqrt{2}$
d) $M\left(-\frac{1}{2}, \frac{1}{2}\right)$, $L = \sqrt{2}$ e) $M\left(\frac{1}{2}, -\frac{1}{2}\right)$, $L = \sqrt{3}$

5) What is the equation of the line having a slope of 0 and passing through the point $(-6, -1)$?

- a) $x = -6$ b) $x = -1$ c) $y = -6$
d) $y = -1$ e) $y = \frac{1}{6}$

6) Factor: $2x^2 + 11x + 15$

- a) $(2x+3)(x+5)$ b) $(x+3)(x+5)$ c) $(2x+15)(x+1)$
d) $(2x+5)(x+3)$ e) $(2x+1)(x+15)$

7) The expression $x^2 - 10kx + R$ is a perfect square. Find the value of R .

- a) 25 b) $5k^2$ c) $25k^2$
d) $100k^2$ e) $25k^2x^2$

8) Consider solving $x^2 + 12x + 5 = 0$ by completing the square: $x^2 + 12x + \underline{\hspace{1cm}} = -5 + \underline{\hspace{1cm}}$
What is the number that goes in the blanks?

- a) 144 b) 36 c) 16 d) -16 e) -36

9) Solve $3x^2 - 5x - 1 = 0$ using the Quadratic Formula.

- a) $\frac{-10 \pm \sqrt{101}}{3}$ b) $\frac{-5 \pm \sqrt{37}}{6}$ c) $\frac{5 \pm \sqrt{37}}{6}$

d) $\frac{10 \pm \sqrt{101}}{9}$

e) $\frac{10 \pm \sqrt{101}}{3}$

10) The graph of the parabola $y = x^2 + 6x + 13$ is symmetric about a line. What is the equation of that line?

a) $x = -3$

b) $x = 0$

c) $x = 3$

d) $y = 0$

e) $y = 3$

11) What is the equation of the circle centered at $(4, -5)$ with a radius of 16?

a) $(x + 4)^2 + (y - 5)^2 = 16$

b) $(x - 4)^2 + (y + 5)^2 = 4$

c) $(x + 4)^2 + (y - 5)^2 = 256$

d) $(x - 4)^2 + (y + 5)^2 = 256$

e) $(x + 4)^2 + (y - 5)^2 = 4$

12) Determine which of the following triangles are right triangles if the sides' lengths are:

I) 8, 15, 17

II) 4, 5, 6

III) 2, 2, 3

IV) 9, 12, 15

a) I only

b) II only

c) III only

d) I and IV only

e) I, II and IV

13) A triangle ABC has right angle B. Sides AB and BC have the lengths 3 and 4 respectively. Determine the cosine of angle A ($\cos A$).

a) $\frac{3}{5}$

b) $\frac{3}{4}$

c) $\frac{4}{5}$

d) $\frac{4}{3}$

e) $\frac{5}{3}$

14) Which of the following ratios is the tangent of an angle?

a) $\frac{\text{opposite}}{\text{hypotenuse}}$

b) $\frac{\text{hypotenuse}}{\text{adjacent}}$

c) $\frac{\text{adjacent}}{\text{hypotenuse}}$

d) $\frac{\text{hypotenuse}}{\text{opposite}}$

e) $\frac{\text{opposite}}{\text{adjacent}}$

15) What is the value of $\sin \frac{2\pi}{3}$?

a) $\frac{1}{2}$

b) $-\frac{1}{2}$

c) $\frac{\sqrt{3}}{2}$

d) $\frac{-\sqrt{3}}{2}$

e) $\frac{\sqrt{2}}{2}$

16) What is the value of $\cot \frac{3\pi}{2}$?

a) 0

b) 1

c) -1

d) $\frac{\sqrt{2}}{2}$

e) does not exist

17) What is the value of $\log_2 64$?

a) 6

b) 8

c) 16

d) 128

e) 4096

18) Which of the following is equal to $\log_k A = \frac{3}{2}$?

a) $k = \sqrt[3]{A}$

b) $k = \left(\frac{3}{2}\right)^A$

c) $\frac{3}{2} = \sqrt[4]{A}$

d) $A = \sqrt{\frac{3}{2}}$

e) $A = \sqrt{k^3}$

19) Write as a single logarithm: $\log_8 5 - 2\log_8 6$

- a) $\log_8 \frac{5}{36}$ b) $\log_8 \frac{5}{12}$ c) $\log_8 11$ d) $\log_8 41$ e) $\log_8 180$

20) What is the result when $\log \frac{AB}{\sqrt{C}}$ is expanded?

- a) $\log A + \frac{1}{2}(\log B - \log C)$ b) $\frac{1}{2}(\log A + \log B - \log C)$
c) $\log A + \log B - 2 \log C$ d) $\frac{1}{2}(\log A \log B - \log C)$
e) $\log A + \log B - \frac{1}{2} \log C$