Instructor: Dr. A. Atoyan, Office: LB 1041-24 (SGW)  
Email: armen.atoyan@concordia.ca

Office hours: Wednesday 12:00-13:30, Thursday 13:30-14:30.


Prerequisites: MATH 204 or equivalent is a prerequisite for this course.

Objective: This is the first part of the two connected Linear Algebra and Applications courses, the second part being MAST 235. There are two major concepts, Vector Spaces and Linear Transformations, on which this first part is based. In learning these concepts we will use related constructs such as vectors, matrices and systems of linear equations. The objective of the course is to master your understanding and skills in these key concepts of Linear Algebra that will be critical for further Linear Algebra courses in your curriculum.

Pedagogy: Classes are interactive, and start with a lecture introducing the principal concepts of the topic considered, followed by problem solving by students in the lab equipped with computers. Mathematical issues that arise during problem solving are discussed in class.

Software: The software used in this course is Maple. The Waterloo’s Maplesoft is making "Maple Student’s edition” available to Concordia students at a special price. In this course the software is only used as a computational tool, not as an object of study in itself. All assignments, quizzes, the midterm test and the final examination are done using Maple.

Assignments: Assignments are given and submitted online through Moodle. Late assignments will not be accepted. Assignments contribute 10% to your final grade (see the Grading Scheme). Working regularly on the assignments, as well as class attendance and working on the problems in the class, is essential for success in this course.
Midterm Test: There will be one midterm test, based on the material of weeks 1-6 (see Contents below), which will contribute up to 25% to your final grade (see the Grading Scheme). It will be held in class on Tuesday March 5, 2019.

NOTE: It is the Department’s policy that tests missed for any reason, including illness, cannot be made up. If you missed the midterm because of illness (to be confirmed by a valid medical note) the final exam can count for 85% of your final grade, and 15% will be contributed by the assignments and the quizzes.

Final Exam: The Final Examination will be 3 hours long (closed-book exam, no notes or electronic material is allowed) written using MAPLE in the lab equipped with computers. Students are responsible for finding out the date and time of the final exam once the schedule is posted by the Examinations Office. Conflicts with the schedule of the final exam must be reported directly to the Examinations Office, not to the Instructor. Students are to be available until the end of the final exam period. Conflicts due to travel plans will not be accommodated.

NOTE: There are no supplemental exams for this course.

Grading Scheme: The final grade will be based on the higher of (a) and (b) below:

(a) 10% for the assignments
   5% for the best 2 of 3 quizzes (see the schedule below)
   25% for the class test
   60% for the final examination

(b) 10% for the assignments
   5% for the best 2 of 3 quizzes
   10% for the class test
   75% for the final examination

If the grading scheme for this course includes graded assignments, a reasonable and representative subset of each assignment may be graded. Students will not be told in advance which subset of the assigned problems will be marked and should therefore attempt all assigned problems.

IMPORTANT: NOTE that there is NO "100% FINAL EXAM" option in this course. The term work contributes at least 25% to the final grade. Therefore, active participation in classes and continuous work on the course material during the semester is essential for success in this course.

Disclaimer: The instructor reserves the right to make changes to the course outline and course content should this be necessary for academic or other reasons. Every effort will be made to minimize such changes.
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LINEAR SYSTEMS & MATRICES | • Review of systems of linear equations.  
  - Matrix form of a system  
  - Matrix of the system; augmented matrix  
  - Elementary Row Operations  
  - Row Echelon Form  
  - Row equivalent matrices  
  - Solutions for a system of linear equations; systems with parameters | Gen.Ex. 1.1  
# 5, 23, 35, 39 |
| 2    | Section 1.2  
VECTORS, MATRICES, SPANS | • Review of vectors and matrices  
  - Vectors in $\mathbb{R}^n$. Linear combination of vectors  
  - Matrix-vector products  
  - Span of a set of vectors  
  - Consistency of systems of linear equations in terms of span of columns of the matrix | Gen.Ex. 1.2  
# 11, 15, 19, 25 |
| 3    | Section 1.3  
HOMOGENEOUS SYSTEMS | • Homogeneous systems of equations, and the  
  - Null Space of a matrix  
  - The rank of a matrix  
  - Nontrivial solutions of a homogeneous system.  
  - Linear dependence of vectors and  
  - homogeneous systems of equations | G.Ex. 1.3  
# 5, 9, 13, 21, 25 |
| 4    | Sections 2.1, 2.4, 5.1  
VECTOR SPACES and SUBSPACES | • Examples of Vector Spaces  
  - n-tuples ($\mathbb{R}^n$) & Euclidean vector spaces  
  - Polynomials as vectors  
  - Other examples (Matrices, Functions)  
  - Generalization: the axioms of a vector space.  
  - Properties of vector spaces (Theorems 2.4: 1-5)  
  - Linear Independence in general vectors spaces.  
  - Vector Subspaces: Definition, Properties, Examples | G.Ex. 2.1:  
# 1, 7, 11, 13, 23  
G.Ex. 2.4  
# 7, 15, 27, 33, 35  
G.Ex. 5.1  
# 1, 3, 5, 11, 15, 29 |
| 5    | Section 3.1  
OPERATIONS ON MATRICES, DETERMINANTS | • Operations on matrices  
  - Matrix addition and scalar multiplication  
  - Multiplication of matrices: definition and properties  
  - Special matrices  
  - Determinants (an introductory overview) | G.Ex. 3.1  
#11, 19, 41, 47, 51 |
| 6    | Section 3.2  
MATRIX INVERSES (Left, Right, & Invertible) | • Left and Right inverses of Matrices.  
  • Square matrices: definition of an invertible matrix  
  • Properties of invertible matrices. | G.Ex. 3.2  
# 9, 11, 19, 21 |
| 7    | Section 2.3  
LINEAR TRANSFORMATIONS IN $\mathbb{R}^n$ | • Linear transformations in $\mathbb{R}^n$  
  - Domain, Co-domain, Range: definition and examples  
  - The Linearity properties: definition and examples  
  - Matrices and linear maps: Theorems 1-3.  
  - Composition of linear mappings (Theorem 2.3.8) | G.Ex. 2.3  
# 3, 7, 9, 11, 21, 15, 25, 43 |
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Academic Integrity and the Academic Code of Conduct
This course is governed by Concordia University's policies on Academic Integrity and the Academic Code of Conduct as set forth in the Undergraduate Calendar and the Graduate Calendar. Students are expected to familiarize themselves with these policies and conduct themselves accordingly. "Concordia University has several resources available to students to better understand and uphold academic integrity. Concordia’s website on academic integrity can be found at the following address, which also includes links to each Faculty and the School of Graduate Studies: concordia.ca/students/academic-integrity." [Undergraduate Calendar, Sec 17.10.2]