Department of Mathematics & Statistics
Concordia University

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MATH 203
Differential & Integral Calculus I
Summer 2015

</div>

Instructor*: _____

Office/Tel No.: _____

Office Hours: _____

*Students should get the above information from their instructor during class time. The instructor is the person to contact should there be any questions about the course.

Course Examiner: Dr. A. Atoyan

Text: *Single Variable Calculus*, by J. Stewart, 8th Edition (Customized), Nelson Education.

Prerequisite: Math 201 or an equivalent Functions course.

Tutorials: Calculus requires a lot of practice. There is not enough class time to do all the examples and problems needed to learn the material thoroughly. The Department has therefore organized special *calculus Tutorials* conducted once per week for every section of this course to provide additional support to students outside the lecture room environment. Tutorials are conducted by senior students who will help with solving problems on the topics learned in class that week, with particular emphasis on the material that students may have difficulties with in this course. Students are strongly encouraged to participate and be active at these problem-solving sessions with represent an important resource to help to succeed in this course.

WeBWorK: Every student will be given access to an online system called **WeBWorK**. The system provides you with many exercises and practice problems. Students will use this system to do online assignments. Students also are strongly encouraged to use this resource to work on the Practice problem sets - problems similar to the assignment problems, and in areas where they may need extra assistance.

Math Help Centre: In addition to Tutorial classes, a Math Help Centre staffed by graduate students has been organized to help students in solving problems on every-day bases. A schedule of its operation and its location will be posted in the Department.

Office Hours: Your professor will announce her/his office hours during which she/he will be also available to give a reasonable amount of help. Note, however, that if you missed a class it is not reasonable to expect your professor to cover the missed material for you.

Assignments: Students are expected to submit assignments online using **WeBWorK**. Late assignments *will not* be accepted WeBWorK assignments contribute 10% to your final grade (see the **Grading Scheme** below). Working regularly on the assignments is essential for success in this course. Students are also strongly encouraged to do as many problems on their own as their time permits from the list of recommended problems included in this outline as well as the practice problems in WeBWorK mentioned above. A solutions manual for all odd-numbered questions is packaged with the textbook.

Midterm Test: There will be one midterm in Week 4 which will contribute up to 25% to your final grade (see the Grading Scheme below).
NOTE: It is the Department's policy that tests missed for any reason, *including illness,* cannot be made up. If you miss a test because of illness *(to be confirmed by a valid medical note)* the final exam can count for 90% of the final grade, and 10% will be contributed by the assignments.

Final Exam: The final examination will be three hours long.
NOTE: Students are responsible for finding out the date and time of the final exams once the schedule is posted by the Examinations Office. Conflicts or problems with the scheduling of the final exam must be reported directly to the Examinations Office, **not** to your instructor. It is the Department's policy and the Examinations Office's policy that *students are to be available until the end of the final exam period. Conflicts due to travel plans will not be accommodated.*

Grading Scheme: The final grade will be based on the higher of (a) or (b) below:

a) 10% for the WeBWorK assignments,
 25% for the midterm test,
 65% for the final exam.

b) 10% for the WeBWorK assignments,
 10% for the midterm test,
 80% for the final exam.

IMPORTANT: <u>**PLEASE NOTE THAT THERE IS NO "100% FINAL EXAM" OPTION IN THIS COURSE**</u>.
The term work contributes at least 20% to the final grade. Therefore active participation in classes and continuous work on the course material *during* the semester is incremental for the success in this course. Also note that although class attendance is not mandatory, years of experience has shown that students who do not attend classes and believe they can keep up with the material on their own do poorly on the final examination.

Calculators: Only calculators approved by the Department (with a sticker attached as proof of approval) are permitted in the class test and final examination. The preferred calculators are the **Sharp EL 531** and the **Casio FX 300MS,** available at the Concordia Bookstore.
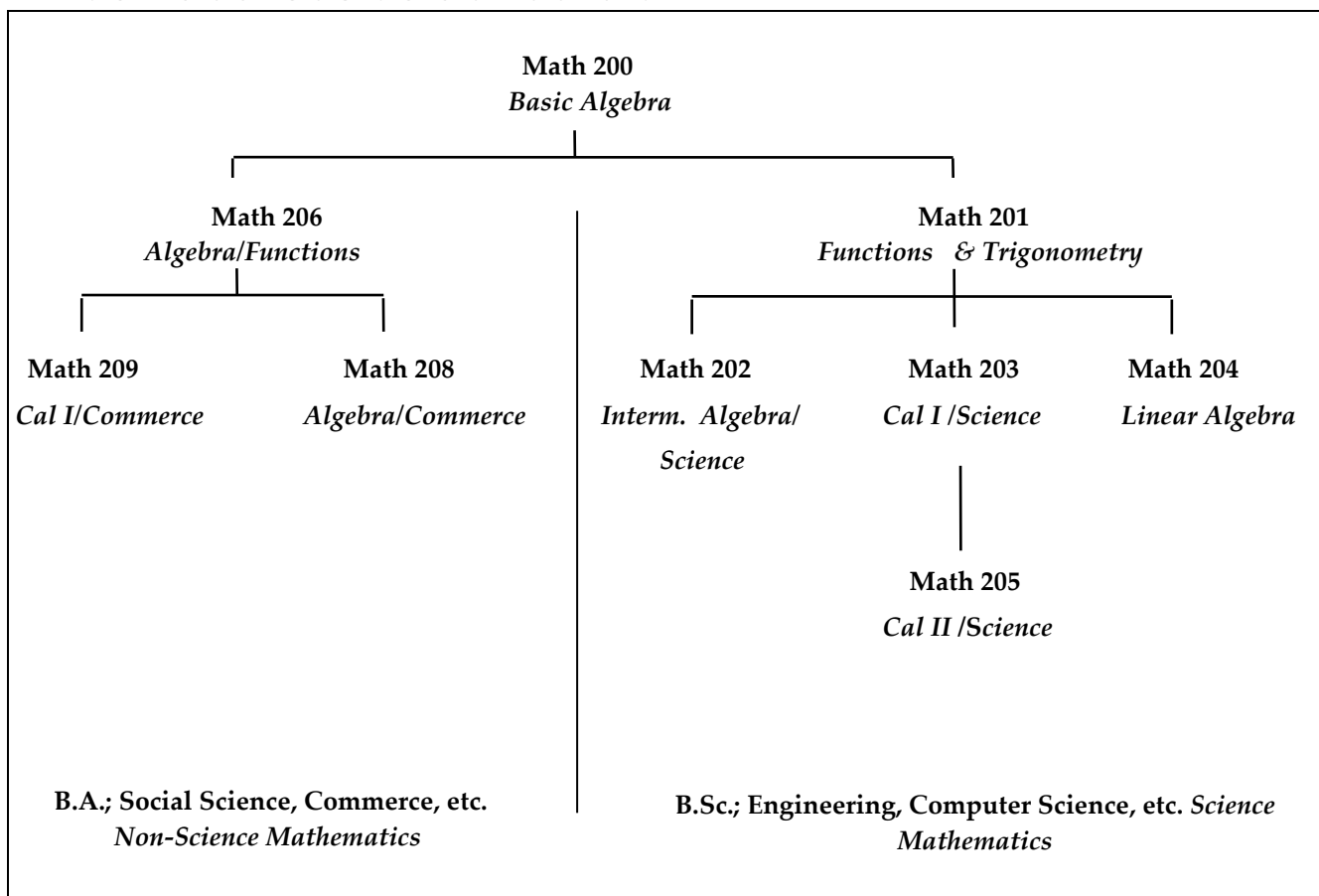
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Note:	All of Chapter 1 is a review of material that was covered in prerequisite courses, and is important for this course. The material that is skipped in this review will be introduced briefly later in the course when needed. <u>If you don't know this preliminary material thoroughly, it is particularly important that you learn it through assignment questions and recommended problems.</u> If you still feel you don't know it well enough after the first class or so (you should also try the quiz at the very end of this document) you may want to consider dropping the course and taking MATH 201 instead.

Weeks/Lectures		Topics		Recommended Problems
1/1	1.1	Representations of functions	p.19:	3, 23, 29, 33, 49, 51
(Review of	1.2	A catalogue of functions	p.33	1, 9, 13, 15
functions)	1.3	New functions from old	p.42:	11, 23, 33, 35, 43
1/2	2.1	The tangent and velocity problems	p.86:	3, 5, 7
	2.2	Limit of a function	p.96:	7, 11, 21, 33
	2.3	Calculating limits	p.106:	11, 17, 27, 45, 63
	2.6	Limits at infinity, horizontal asymptotes	p.140:	19, 21, 27, 29, 45
2/3	2.5	Continuity	p.127:	3, 21, 23, 41
	2.7	Derivatives and rates of change	p.150:	7, 23, 31, 39
	2.8	Derivative as a function; higher derivatives	p.162:	21, 25, 37, 53
2/4	1.5	Exponential functions	p.57:	3, 11, 17, 21, 23
	1.6	Inverse and logarithmic functions	p.69:	9, 11, 21, 37 41, 57
3/5	3.1	Derivatives of polynomials and exp.	p.181:	9, 17, 21, 29, 43, 47
	3.2	Product and quotient rules	p.189:	3, 13, 19, 27
	App. D	Trigonometric functions (an overview)	p.A32	3, 9, 13, 49, 65, 69
3/6	3.3	Derivatives of trigonometric functions	p.197:	3, 7, 11, 23, 25
	3.4	Chain Rule	p.205:	13, 23, 31, 33, 35, 53
4		**MIDTERM TEST**		
		(based on the material of weeks 1-3)		
4/7	3.5	Implicit differentiation	p.215:	9, 17, 27, 29, 39
	3.6	Derivatives of logarithmic functions	p.223:	7, 19, 23, 43, 45
5/8	3.8	Exponential growth/decay	p.242	3, 9, 11, 17, 19
	3.9	Related rates	p.248:	3, 5, 11, 13, 15, 23, 33
5/9	3.10	Linear approximations, differentials	p.255:	1, 5, 11, 13, 17, 19, 33, 37
	4.1	Maximum/minimum values	p.280:	25, 31, 37, 43, 51, 61
6/10	4.2	Mean Value Theorem	p.288:	3, 9, 17, 19, 25
	4.4	Indeterminate forms; L'Hôpital's Rule	p.307:	11, 17, 19, 41, 51
6/11	4.3	Shape of graphs	p.297:	9, 11, 15, 19, 21
	4.5	Summary of curve sketching	p.317:	5, 13, 23, 29, 45
7/12	4.7	Optimization problems	p.331:	13, 15, 19, 23, 29, 33, 37
7		**REVIEW**		

Choosing Between Math 201 and Math 203

If the last math course you took was at the high school level (Quebec), and more than five years have passed since, you should probably register for Math 200. If you are still unsure of your level, read on.

Math Courses at Concordia

Math 200
Basic Algebra

Math 206
Algebra/Functions

Math 201
Functions & Trigonometry

Math 209
Cal I/Commerce

Math 208
Algebra/Commerce

Math 202
Interm. Algebra/ Science

Math 203
Cal I /Science

Math 204
Linear Algebra

Math 205
Cal II /Science

B.A.; Social Science, Commerce, etc.
Non-Science Mathematics

B.Sc.; Engineering, Computer Science, etc. *Science Mathematics*

A self-administered test to help you decide between Math 201 and Math 203 follows. Give yourself about 30 minutes to complete the test. Be honest with yourself, since registering in the wrong course may cost you money and result in a poor grade. Remember that all university-level courses usually demand quite a bit of your time. Students in Math 203 will find they will not have time once the course begins to review material that they are expected to know before they enter the course.

Scoring: 10 or less = Math 201; 11-14 = see an advisor; 15 or better = Math 203. Answers are on the last page.

MATH 203
Qualifying Test

1) What is the equation, in *slope--intercept* form, of the line whose slope is 7 and whose *y-intercept* is -3?

   a) $y = -3x + 7$ b) $y = 7x - 3$
   c) $y = 7x + 21$ d) $y = 7x - 21$
   e) $y = -7x + 3$

2) What is the slope of any line *parallel* to the line $5x + 6y = 30$?

   a) $-\dfrac{6}{5}$ b) $-\dfrac{5}{6}$ c) 0 d) $\dfrac{5}{6}$ e) $\dfrac{6}{5}$

3) The lines $-4x + 5y = -10$ and $5x + ky = 12$ are perpendicular. What is the value of k?

   a) -5   b) -4   c) 4   d) 5   e) 10

4) Find the coordinates of the *midpoint M*, and the *length L* of the line segment joining the points (3, -2) and (4, ◉1). Answer in simple radical form.

   a) $M\left(\dfrac{7}{2}, -\dfrac{3}{2}\right)$, $L=\sqrt{2}$ b) $M\left(\dfrac{7}{2}, \dfrac{3}{2}\right)$, $L=\sqrt{3}$ c) $M\left(\dfrac{1}{2}, -\dfrac{1}{2}\right)$, $L=\sqrt{2}$

   d) $M\left(-\dfrac{1}{2}, \dfrac{1}{2}\right)$, $L=\sqrt{2}$ e) $M\left(\dfrac{1}{2}, -\dfrac{1}{2}\right)$, $L=\sqrt{3}$

5) What is the equation of the line having a slope of 0 and passing through the point (-6, -1)?

   a) $x = -6$ b) $x = -1$ c) $y = -6$
   d) $y = -1$ e) $y = \dfrac{1}{6}$

6) Factor: $2x^2 + 11x + 15$

   a) $(2x+3)(x+5)$ b) $(x+3)(x+5)$ c) $(2x+15)(x+1)$
   d) $(2x+5)(x+3)$ e) $(2x+1)(x+15)$

7) The expression $x^2 ◉ 10kx + R$ is a perfect square. Find the value of R.

   a) 25   b) $5k^2$ c) $25k^2$
   d) $100k^2$ e) $25k^2x^2$

8) Consider solving $x^2 + 12x + 5 = 0$ by completing the square: $x^2 + 12x + \underline{\quad} = -5 + \underline{\quad}$
   What is the number that goes in the blanks?

   a) 144   b) 36   c) 16   d) -16   e) -36

9) Solve $3x^2 - 5x - 1 = 0$ using the Quadratic Formula.

   a) $\dfrac{-10 \pm \sqrt{101}}{3}$ b) $\dfrac{-5 \pm \sqrt{37}}{6}$ c) $\dfrac{5 \pm \sqrt{37}}{6}$

   d) $\dfrac{10 \pm \sqrt{101}}{9}$ e) $\dfrac{10 \pm \sqrt{101}}{3}$

10) The graph of the parabola $y = x^2 + 6x + 13$ is symmetric about a line. What is the equation of that line?

   a) $x = -3$ b) $x = 0$ c) $x = 3$
   d) $y = 0$ e) $y = 3$

11) What is the equation of the circle centered at (4, ⊙5) with a radius of 16?

   a) $(x + 4)^2 + (y - 5)^2 = 16$ b) $(x - 4)^2 + (y + 5)^2 = 4$
   c) $(x + 4)^2 + (y - 5)^2 = 256$ d) $(x - 4)^2 + (y + 5)^2 = 256$
   e) $(x + 4)^2 + (y - 5)^2 = 4$

12) Determine which of the following triangles are right triangles if the sides' lengths are:
   I) 8, 15, 17 II) 4, 5, 6   III) 2, 2, 3   IV) 9, 12, 15

   a) I only   b) II only   c) III only   d) I and IV only   e) I, II and IV

13) A triangle ABC has right angle B. Sides AB and BC have the lengths 3 and 4 respectively. Determine the cosine of angle A ($\cos A$).

   a) $\dfrac{3}{5}$ b) $\dfrac{3}{4}$ c) $\dfrac{4}{5}$ d) $\dfrac{4}{3}$ e) $\dfrac{5}{3}$

14) Which of the following ratios is the tangent of an angle?

   a) $\dfrac{\text{opposite}}{\text{hypotenuse}}$ b) $\dfrac{\text{hypotenuse}}{\text{adjacent}}$ c) $\dfrac{\text{adjacent}}{\text{hypotenuse}}$

   d) $\dfrac{\text{hypotenuse}}{\text{opposite}}$ e) $\dfrac{\text{opposite}}{\text{adjacent}}$

15) What is the value of $\sin \dfrac{2\pi}{3}$?

   a) $\dfrac{1}{2}$ b) $-\dfrac{1}{2}$ c) $\dfrac{\sqrt{3}}{2}$ d) $\dfrac{-\sqrt{3}}{2}$ e) $\dfrac{\sqrt{2}}{2}$

16) What is the value of $\cot \dfrac{3\pi}{2}$?

    a) 0   b) 1   c) -1   d) $\dfrac{\sqrt{2}}{2}$ e) does not exist

17) What is the value of $\log_2 64$?

    a) 6   b) 8   c) 16   d) 128   e) 4096

18) Which of the following is equal to $\log_k A = \dfrac{3}{2}$?

    a) $k = \sqrt[3]{A}$ b) $k = \left(\dfrac{3}{2}\right)^A$ c) $\dfrac{3}{2} = \sqrt[k]{A}$ d) $A = \sqrt[k]{\dfrac{3}{2}}$ e) $A = \sqrt{k^3}$

19) Write as a single logarithm: $\log_8 5 - 2\log_8 6$

    a) $\log_8 \dfrac{5}{36}$ b) $\log_8 \dfrac{5}{12}$ c) $\log_8 11$ d) $\log_8 41$ e) $\log_8 180$

20) What is the result when $\log \dfrac{AB}{\sqrt{C}}$ is expanded?

    a) $\log A + \dfrac{1}{2} (\log B - \log C)$ b) $\dfrac{1}{2} (\log A + \log B - \log C)$

    c) $\log A + \log B - 2\log C$ d) $\dfrac{1}{2} (\log A \log B - \log C)$

    e) $\log A + \log B - \dfrac{1}{2} \log C$

ANSWERS: 1. b); 2. b); 3. c); 4. a); 5. d); 6. d); 7. c); 8. b); 9. c); 10. a); 11. d); 12. d); 13. a); 14. e); 15. c); 16. a); 17. a); 18. e); 19. a); 20. e)