# **Department of Mathematics & Statistics Concordia University**

# MATH 201 Elementary Functions Summer 2014

Instructor*:		
Office/Tel No.:		
Office Hours:		

**Course Examiner:** Dr. A. Atoyan.

**Textbook:** *Precalculus Esentials*, by J. Ratti and M. McWaters, Pearson Education.

Office Hours: Your professor will announce her/his office hours during which she/he also will

be available to give a reasonable amount of help. However, if you missed a class it is not reasonable to expect your professor to cover the missed material for you.

**Tutorials:** The material in this course requires a lot of practice. There is not enough class

time to do all the examples and problems needed to learn the material thoroughly. The Department has therefore organized special *Tutorials* conducted once per week for one hour for every section of this course to provide additional support to students outside the lecture room environment. Tutorials are conducted by senior students who will help with solving problems on the topics learned in class that week, with particular emphasis on the material that students may have difficulties with in this course. Some quizzes contributing up to 3 bonus marks to the grade will be given at the Tutorial sessions (see below). Students are strongly encouraged to participate and be active at these problem-solving sessions which represent an important new resource to help you succeed

in this course.

**Math Help Centre:** In addition to Tutorial sessions, a Math Help Centre staffed by graduate students

is available. The schedule of its hours of operation and its location will be posted

in the Department.

**WeBWorK:** Every student will be given access to an online system called **WeBWorK**. The

system provides you with many exercises and practice problems. Students will use this system to do online assignments (see **Assignments** below). In addition, before the midterm test and a few weeks before the end of the course, a number of practice problems will be posted in WeBWorK to help you review the material.

<sup>\*</sup>Students should get the above information from their instructor during class time. The instructor is the person to contact should there be any questions about the course.

#### **Assignments:**

Students are expected to submit assignments online using **WeBWorK**. Late assignments *will not* be accepted. WeBWorK assignments contribute 10% to your final grade (see the **Grading Scheme** below). Besides these online assignments there will be Tutorial quizzes, to be submitted on paper, that will contribute up to 3% bonus marks to the final grade. Working regularly on the assignments is essential for success in this course. Students are also strongly encouraged to do as many problems on their own as their time permits from the list of recommended problems included in this outline as well as the practice problems in WeBWorK mentioned above.

#### **Midterm Test:**

There will be one **midterm test** in Week 4 (based on the material of weeks 1-3) which will contribute up to 25% to your final grade (see the Grading Scheme below).

**NOTE:** It is the Department's policy that tests missed for any reason, *including illness*, cannot be made up. If you miss both the midterm and alternate test because of illness (*to be confirmed by a valid medical note*), the final exam can count for 90% of your final grade, and the remaining 10% will be determined by the WeBWorK assignments.

#### **Final Exam:**

The final examination will be three hours long and will cover all the material in the course.

**NOTE:** Students are responsible for finding out the date and time of the final exams once the schedule is posted by the Examinations Office. Any conflict or problems with the scheduling of the final exam must be reported to the Examinations Office, *not* to your instructor. It is the Department's policy and the Examinations Office's policy that *students are to be available until the end of the final examinations period*. Conflicts due to travel plans will *not* be accommodated.

### **Grading Scheme:**

The final grade will be based, in all cases, on the *higher* of the two options:

- a) 10% for the assignments 25% for the midterm test 65% for the final exam.
- b) 10% for the assignments, 10% for the midterm test, 80% for the final exam.

For both schemes an additional 3% (bonus marks) will be available from the Tutorial quizzes.

#### **IMPORTANT:**

# PLEASE NOTE THAT THERE IS NO "100% FINAL EXAM" OPTION IN THIS COURSE.

The term work contributes at least 20% to the final grade. Therefore, active participation in classes and continuous work on the course material *during* the semester is essential for success in this course. Also, note that although class

attendance is not mandatory, years of experience have shown that students who do not attend classes and believe they can keep up with the material on their own do poorly on the final examination.

**Calculators:** 

Only calculators approved by the Department (with a sticker attached as proof of approval) are permitted in the class test and final examination. The preferred calculators are the **Sharp EL 531** and the **Casio FX 300MS**, available at the Concordia Bookstore.

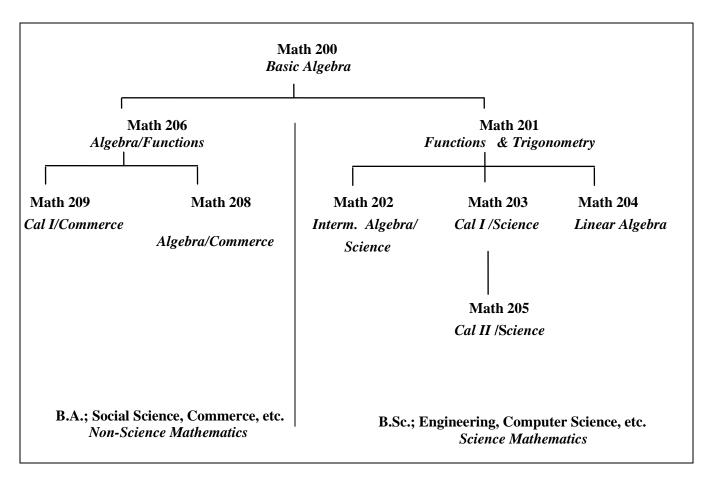
#### **CONTENTS**

Weeks/ Lectures	Sections		Recommended Problems		
1/1	1.1	Graphs of Equations	p. 62	# 5,7,9,17,23,27, 37,55,59,61,69	
	1.2	Lines	p. 74	# 3, 5, 17, 23,29, 31, 53, 55, 65	
1/2	1.3	Functions	p. 90	# 11, 17, 25, 27, 33, 35, 63, 69	
	1.4	A Library of Functions	p. 106	# 9, 17, 19, 29, 31, 47, 51, 57	
	1.5	Transformations of Functions	p. 121	# 3, 5, 11, 19, 33, 51, 63, 67	
2/3	1.6	Combining Functions, Composite	p. 132	# 5, 9, 11, 29, 31, 43, 47, 49	
		Functions			
	1.7	Inverse Functions	p. 144	# 13, 21, 23, 27, 37, 43, 45	
2/4	2.1	Quadratic functions	p. 161	# 7, 9, 17, 21, 29, 45, 47, 61	
	2.5	Rational Functions	p. 211	# 5, 19, 21, 25, 29, 33, 39, 51, 61	
3/5	3.1	Exponential Functions	p. 235	# 5, 9, 13, 23, 31, 47, 51, 53	
	3.2	Logarithmic Functions	p. 250	# 13, 23, 31, 37, 45, 53, 59, 93	
3/6	3.3	Rules of Logarithms	p. 262	# 15, 23, 29, 35, 47, 51, 55, 71, 75	
	3.4	Exponential and Logarithmic Equations	p. 273	# 5, 17, 21, 25, 29, 35, 47, 57, 59	
4		Pre-midterm Review class			
		MIDTERM TEST			
		(based on the material of weeks 1-3)			
5/7	4.1	Angles and Their Measure	p. 290	# 13,15,23,25,45,51,57,63,65,69	
	4.2	The Unit Circle, Trigonometric Functions	p. 307	# 3, 11, 27, 31,37, 57, 67, 75	
5/8	4.3	Graphs of the Sine and Cosine Functions	p. 325	# 13, 17, 23, 25, 33, 37, 41, 43	
	4.5	Inverse Trigonometric Functions	p. 348	# 9,15, 17,25, 35, 55, 59, 61, 71	
6/9	4.6	Right Triangle Trigonometry	p. 358	# 13, 17, 21,31, 35, 39, 41, 47, 53	
	4.7	Trigonometric Identity	p. 370	# 3, 15, 19, 27, 33, 41, 45, 71, 73	
6/10	4.8	Sum and Difference Formulas	p.385	# 1, 3, 13, 21, 29, 33, 41, 45, 51	
	5.1	The Law of Sine and the Law of Cosines	p.407	# 1, 5, 7, 17,23, 27, 31, 49, 61, 65	
7		REVIEW CLASSES			

## **Choosing Between Math 200 and Math 201**

If the last math course you took was at the high school level (Quebec), and more than five years have passed since, you should probably register for Math 200. If you are still unsure of your level, read on.

### **Math Courses at Concordia**



A self-administered test to help you decide between Math 200 and Math 201 follows. Give yourself about 30 minutes to complete the test. Be honest with yourself, since registering in the wrong course may cost you money and result in a poor grade. Remember that all university-level courses usually demand quite a bit of your time. Students in Math 201 will find they will not have time once the course begins to review material that they are expected to know before they enter the course.

<u>Help</u>: The Math Department runs a drop-in **Math Help Centre** in **LB 912** - call the Department's office for further information at 848-2424, Ext. 3222/3223. Counseling and Development runs math skills workshops, 2 or 3 times a week - call the Counseling and Development's office for further information at 848-2424, Ext. 3545/3555.

1) The sum of  $3x^2 + x - 7$  and  $x^2 + 10$  can be expressed as

2) The product of  $(-3xy^2)(5x^2y^3)$  is:

# MATH 201 Qualifying Test

a)  $4x^2 + x - 3$  b)  $3x^2 + x + 3$  c)  $4x^4 + x - 3$  d)  $4x^2 + x + 3$ 

a)  $-8x^3y^5$  b)  $-15x^3y^5$  c)  $-15x^2y^5$  d)  $-15x^3y^6$ 

3) Expressed as a single fraction in lowest terms, the sum of  $\frac{3x}{4}$  and  $\frac{2x}{3}$  is equivalent to:

a)  $\frac{5x}{7}$  b)  $\frac{5x}{12}$  c)  $\frac{17x}{7}$  d)  $\frac{17x}{12}$ 

# Part One

4)	If $15x^6y$ is divided by $-3x^3$ , the quotient is:				
	a) $-5x^2$	$b) -5x^3y$	c) $5x^2$	d) $5x^3y$	
5)	Written in factored form, the binomial $a^2b - ab^2$ is equivalent to:				
	a) $ab(a-b)$	b) $(a - b) (a + b)$	c) $a^2(b-b^2)$	$d) a^2b^2(b-a)$	
6)	The solution set for $2x^2 - 7$	4x - 4 = 0 is:			
	a) {2, 1}	b) $\{-\frac{1}{2},4\}$	c) {-2, 1}	d) $\{\frac{1}{2}, -4\}$	
7)	What is the solution for the $2x + y = 7$ x - 2y = 6	following system of	equations?		
	a) {3, 1}	b) {1, 3}	c) {-1, 4}	d) {4, -1}	
8)	The sum of $\sqrt{12}$ and $5\sqrt{3}$	is:			
	a) 10√3	b) 7√6	c) 7√3	d) 360	
9)	The graph of the line passis	ng through the points	(6, 7) and (4, 2) has	a slope of:	
	a) $\frac{2}{5}$ b)	$-\frac{5}{2}$	c) $\frac{5}{2}$	d) $-\frac{1}{2}$	

a) $y=\frac{1}{2}x-3$ b) $y=\frac{1}{2}x+3$ c) $y=3x+\frac{1}{2}$ d) $y=\frac{1}{2}x+3$ 12) The inequality $3x+2>x+8$ is equivalent to:  a) $x>-\frac{3}{2}$ b) $x>\frac{3}{2}$ c) $x>3$ d) $x<3$ 13) The smallest whole number that satisfies the inequality $3x-1>2$ is:  a) 1 b) 2 c) 3 d) 0  14) If $x$ is an integer, what is the solution set of $3< x \le 6$ ?  a) $\{3,4,5\}$ b) $\{4,5,6\}$ c) $\{3,4,5,6\}$ d) $\{4,5\}$ 15) The lengths of sides of a triangle are 8, 15, and 17. If the longest side of a similar triangle is 51, what is the length of the shortest side?  a) $32$ b) $24$ c) $16$ d) $4$ 16. If two legs of a right triangle are 5 and 12, the hypotenuse is:  a) $\sqrt{119}$ b) $\sqrt{17}$ c) $17$ d) $13$ 17) What is the circumference of a circle whose radius is $6$ ?  a) $6\pi$ b) $12\pi$ c) $36\pi$ d) $3\pi$	10) The graph of the equation $y = 3$ is a line:				
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		a) 2 <i>x</i>	b) $x + 3$	c) $\frac{1}{2}x - 3$	d) $2x + 3$

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# Part Two

1) Simplify: 
$$(2w^3 - 5w - 15) - (-6w^2 + w - 15) + (4w^2 - 7)$$

2) Evaluate: 
$$-r - [-p - (-n + r)]$$
 for  $n = -3$ ,  $p = 4$  and  $r = -1$ 

3) Simplify: 
$$\frac{1}{3^{-1}-4^{-1}}$$

4) Perform the indicated operations: 
$$-\frac{1}{6} + \frac{11}{14}$$

5) Factor completely: 
$$3x^2 - 15x - 42$$

6) Perform the indicated operations and express in simplest form: 
$$\frac{x^2-16}{x^2-x-20} \bullet \frac{1}{x-4}$$

8) Express 
$$\frac{3}{\sqrt{5}+1}$$
 as an equivalent fraction with a rational denominator.

9) Solve: 
$$-14 - 6a < -74$$

11) Solve 
$$x + 5 = 3y - 2$$
  
 $2x + 7 = y + 3$ 

### **ANSWERS**

#### Part One:

#### Part Two:

1. 
$$2w^3 + 10w^2 - 6w - 15 - 7$$
; 2. 7; 3. 12; 4.  $\frac{13}{21}$ : 5.  $3(x - 7)(x + 2)$ ; 6.  $\frac{1}{x - 5}$ ; 7.  $20\sqrt{6}$ ; 8.  $\frac{3(\sqrt{5} - 1)}{4}$ ; 9. a > 10; 10. 4; 11. (-1;2); 12. 6.